

*ISSI-BJ Workshop Oct. 14-18*  
*"Oscillatory Processes in Solar and Stellar Coronae"*

**Problems and challenges  
of studying the non-stationary  
properties of QPPs**

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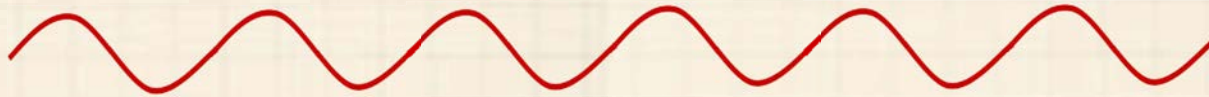
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# Questions of interest

1. QPPs - what are they?  
New terminology:  
what do we mean under  
non-stationarity
2. Three Zoos:
  - Theory
  - Observations
  - Analysis
3. Case study - two events - two types of non-stationarity

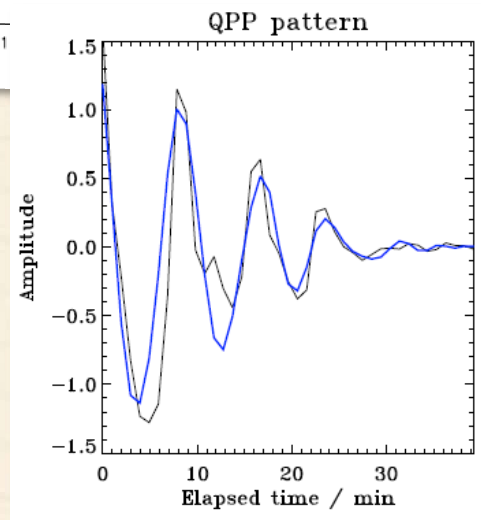
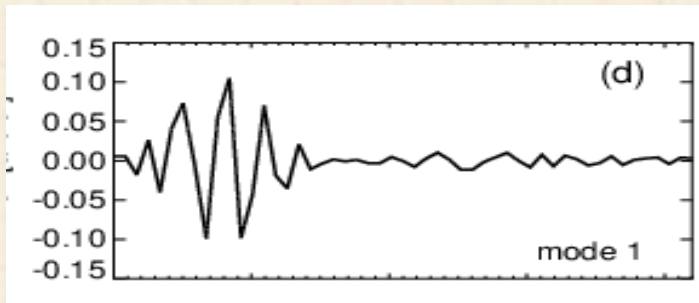
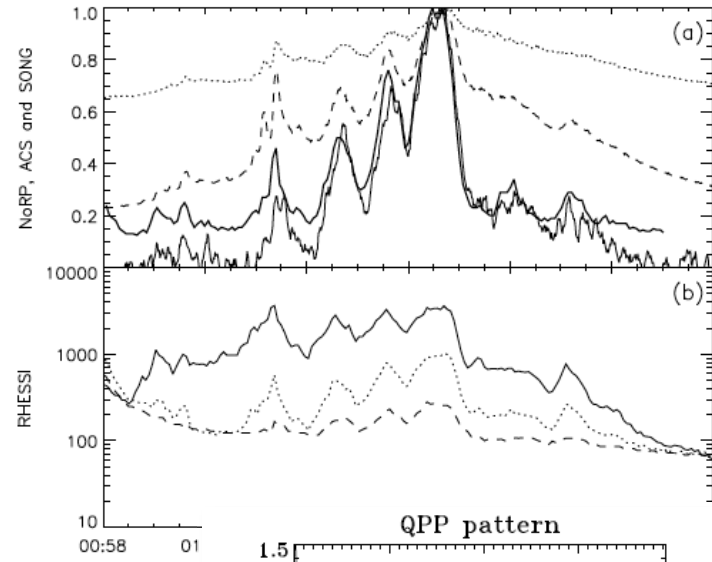
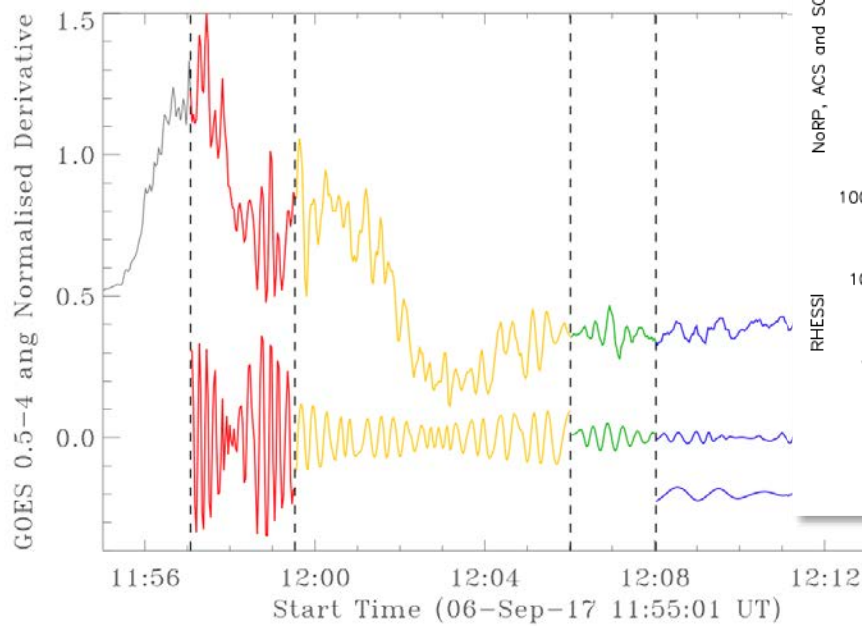
# What do we mean by non-stationary properties?

What is the stationary signal, or Periodic Pulsations (PP)?



Any deviation from the harmonic shape is called Quasi-Periodic Pulsations (QPPs)

# A zoo of deviations from the PP



Periods -> characteristic time scales

# Types of the non-stationarities

Multiple modes'  
interference



Two processes  
going on  
consequently or  
simultaneously

Natural  
non-stationarity



It is associated  
with a time-dependent  
physical process

# Types of the non-stationarities

Multiple modes' interference

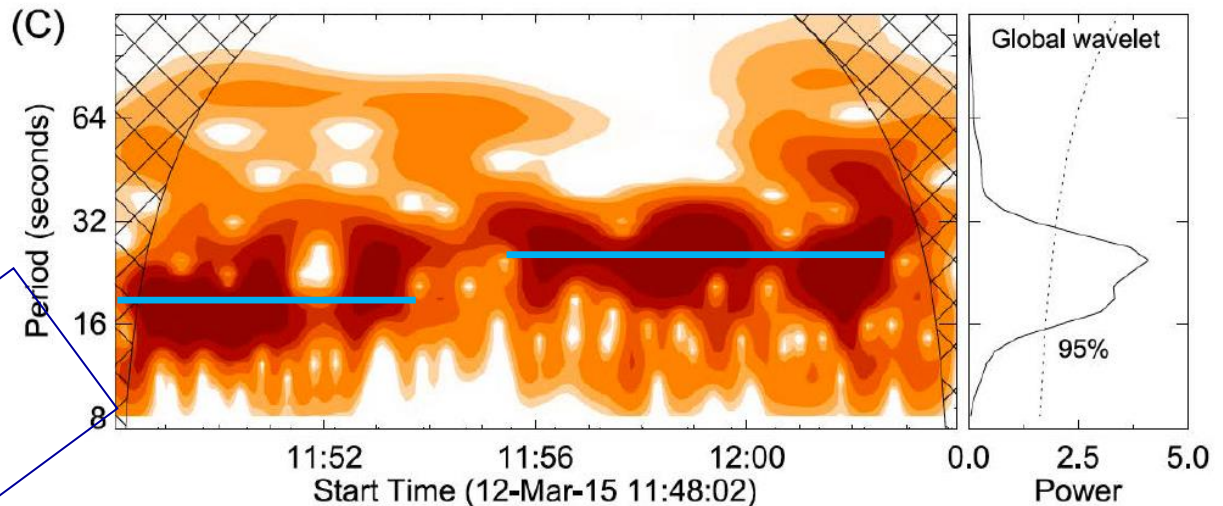
Natural non-stationarity



Two processes going on consequently simultaneously

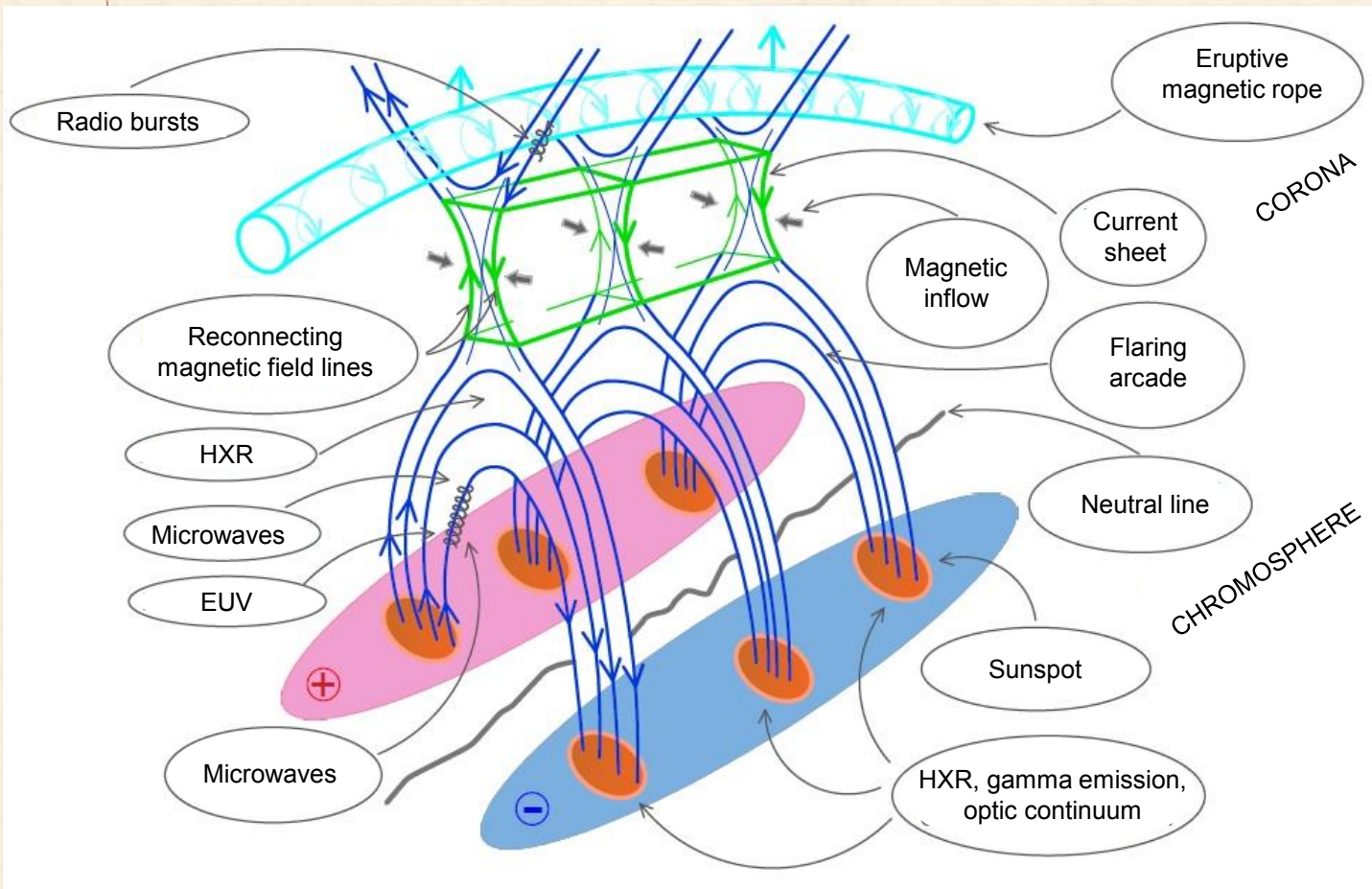
Talk by Hui Tian yesterday

Evolving period



- Two dominant periods at 19 s and 27 s
- The 19 s period: likely not the second harmonic, but caused by change of the loop internal condition ( $N, B, L$ )

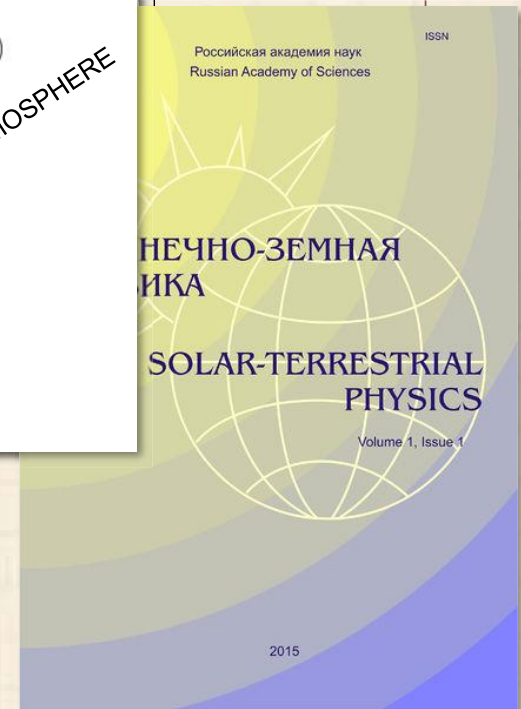
# Mechanisms of QPPs



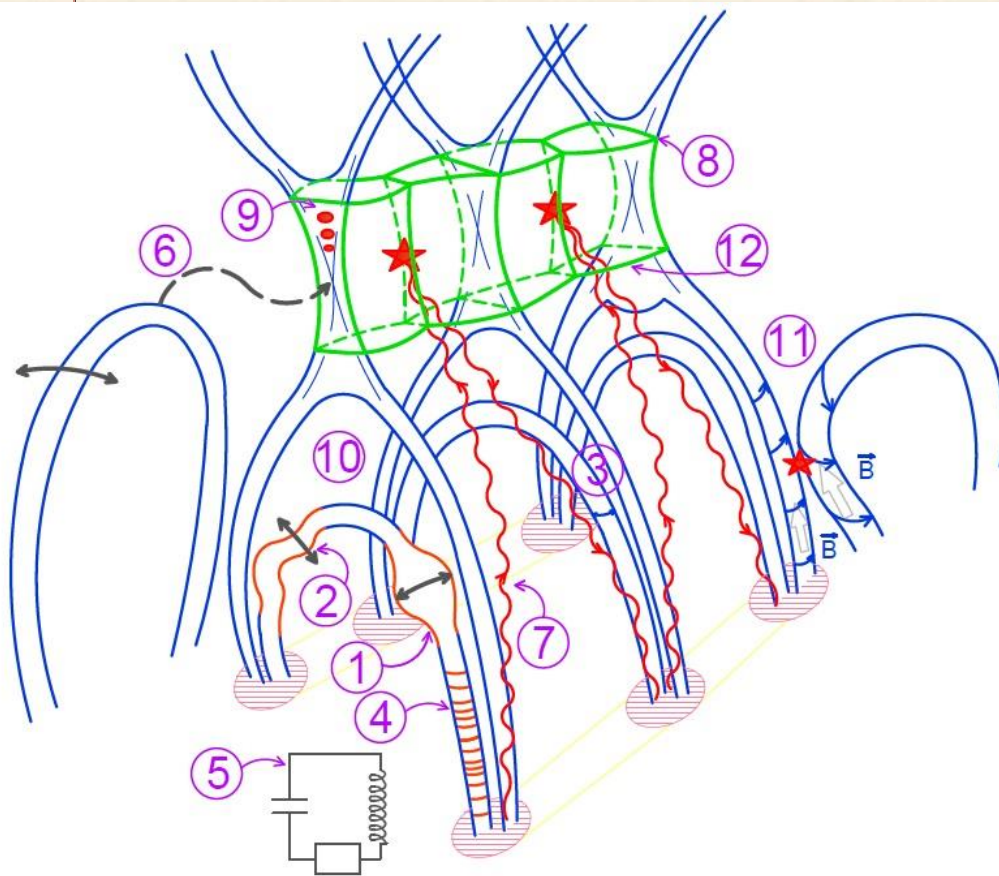
"Quasi-periodic pulsations in solar and stellar flares"

E.G. Kupriyanova, D.Y. Kolotkov,  
V.M. Nakariakov, A.S. Kaufman

STP 2019 (The review is under reviewing)



# Mechanisms of QPPs



- ① Sausage mode  
Nakariakov et al. (2012)
- ② Kink mode
- ③ Torsion mode
- ④ Slow magnetoacoustic mode
- ⑤ RLC contour  
Zaitsev, Stepanov (2008)
- ⑧ Flapping oscillations  
Erkaev et al. (2007)

Zaitsev, Stepanov (1975)  
Edwin, Roberts (1983)

- ⑨ Auto-oscillations  
Murray et al. (2009)  
Nakariakov et al. (2010)
- ⑩ Oscillatory thermal instability  
Zavershinskii et al. (2019)
- ⑪ Oscillatory two-loop coalescence  
Tajima et al. (1987)  
Kolotkov et al. (2016)
- ⑫ Magnetic fork  
Takasao, Shibata (2016)

- ⑥ Periodically induced reconnection  
McLaughlin et al. (2011)
- ⑦ Nakariakov, Zimovets, 2011



# MHD mechanism for non-stationarity

(Zaitsev, Stepanov 1975; Edwin, Roberts 1983; papers of Nakariakov and his team)

Period of the standing MHD wave or of Alfvén wave in a loop:

$$P = \frac{2L}{nv_{\text{ph}}}$$

$L$  is loop length  
 $n$  is a harmonic number  
 $v_{\text{ph}}$  is the phase speed

Dispersion equation of the MHD modes - stationary case:

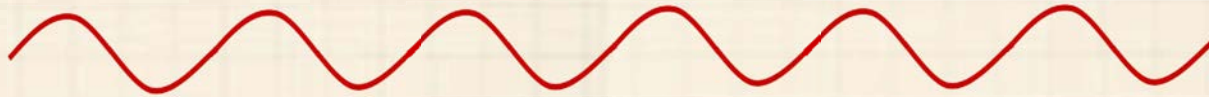
$$\rho_e (v_{\text{ph}}^2 - v_{Ae}^2) \mu_0 \frac{Z'_m(\mu_0 a)}{Z_m(\mu_0 a)} + \rho_0 (v_{A0}^2 - v_{\text{ph}}^2) \mu_e \frac{Z'_m(\mu_e a)}{Z_m(\mu_e a)} = 0.$$

$\left\{ \begin{array}{l} L, a \\ N_o, B_o, T_o \\ N_e, B_e, T_e \end{array} \right.$

Parameters in dispersion equation depend on time.  
Changing of the physical parameters  $\Rightarrow$   
changing the observables, parameters of QPPs  $\Rightarrow$   
**non-stationarity** of the QPPs

# What do we mean by non-stationary properties?

What is the stationary signal, or Periodic Pulsations (PP)?



Any deviation from the harmonic shape is called Quasi-Periodic Pulsations (QPPs)

Really ANY deviation?

What is the upper limit of the deviation allowing not to fall to a noise?

# Methods of analysis of QPPs: time profiles

- Fourier periodogram (of total time series, of the de-trended time series, AFINO code)
- Wavelet transform
- Empirical mode decomposition (EMD)
- Bayesian inference and Markov chains Monte Carlo (talk by Sergey Anfinogentov on Monday)

Significance tests are important !

# Methods of analysis of QPPs: time profiles

A blueprint of state-of-the-art techniques for detecting quasi-periodic pulsations in solar and stellar flares

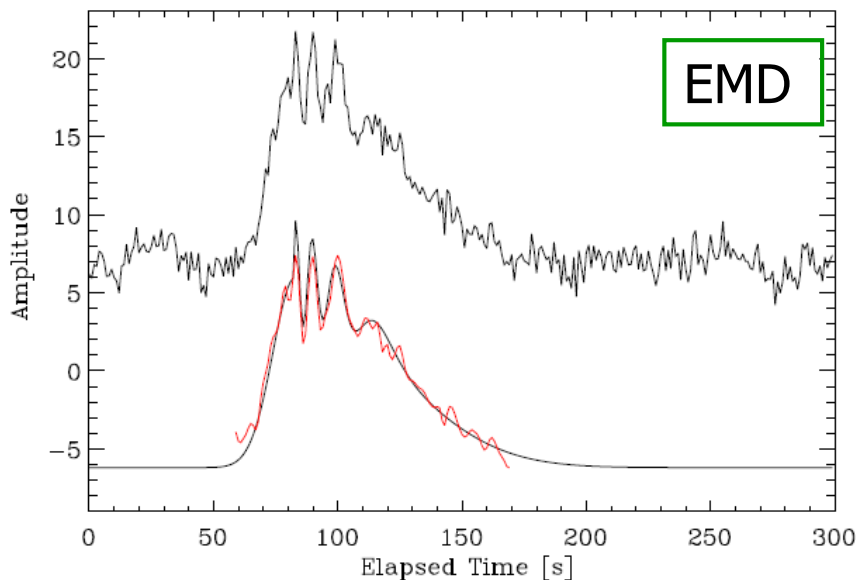
ANNE-MARIE BROOMHALL,<sup>1,2</sup> LAURA A. HAYES,<sup>3</sup> ANDREW R. INGLIS,<sup>4</sup> DMITRII Y. KOLOTKOV,<sup>1</sup> JAMES A. McLAUGHLIN,<sup>5</sup>  
TISHTRYA MEHTA,<sup>1</sup> VALERY M. NAKARIAKOV,<sup>1,6</sup> YUTA NOTSU,<sup>7</sup> DAVID J. PASCOE,<sup>8</sup> CHLOE E. PUGH,<sup>1</sup> AND  
TOM VAN DOORSSELAERE<sup>8</sup>



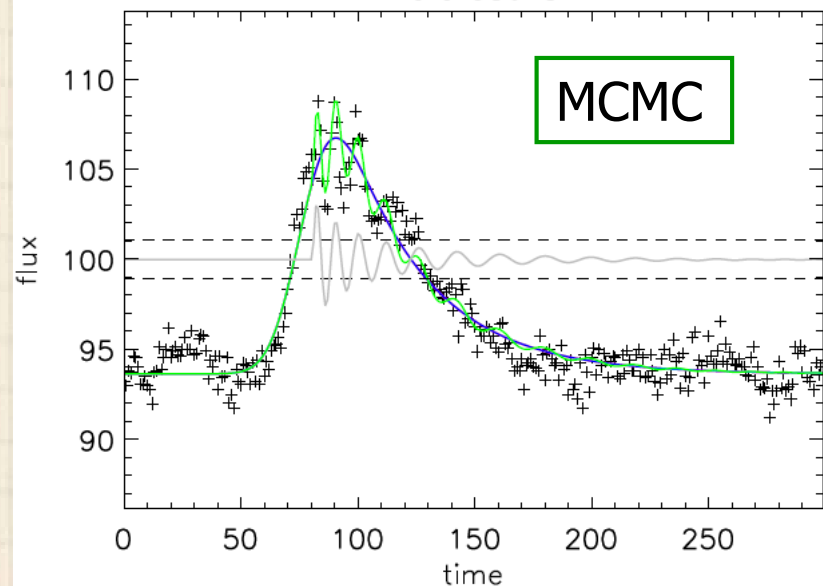
8 methods were tested

**Non-stationarity** is better defined by EMD and MCMC

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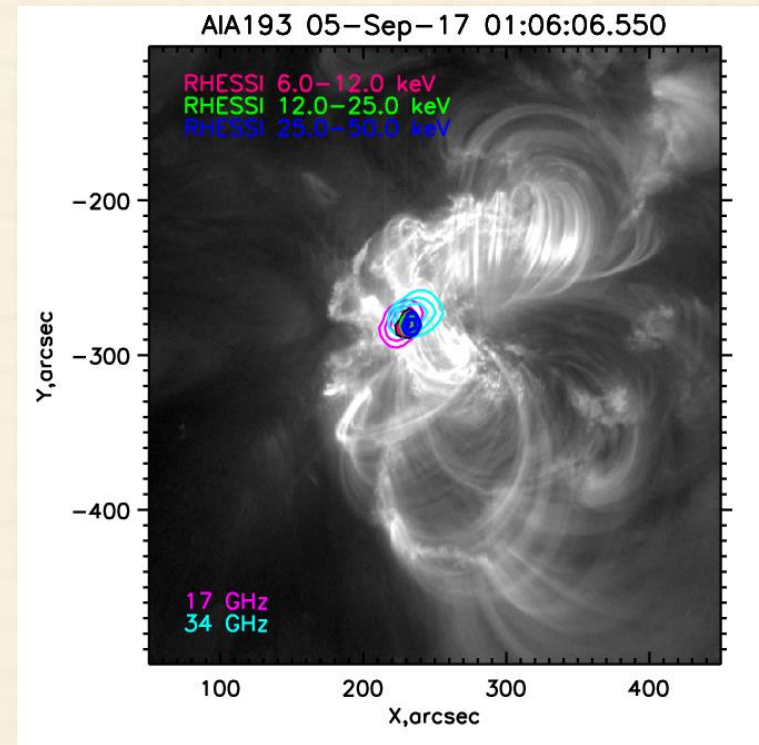
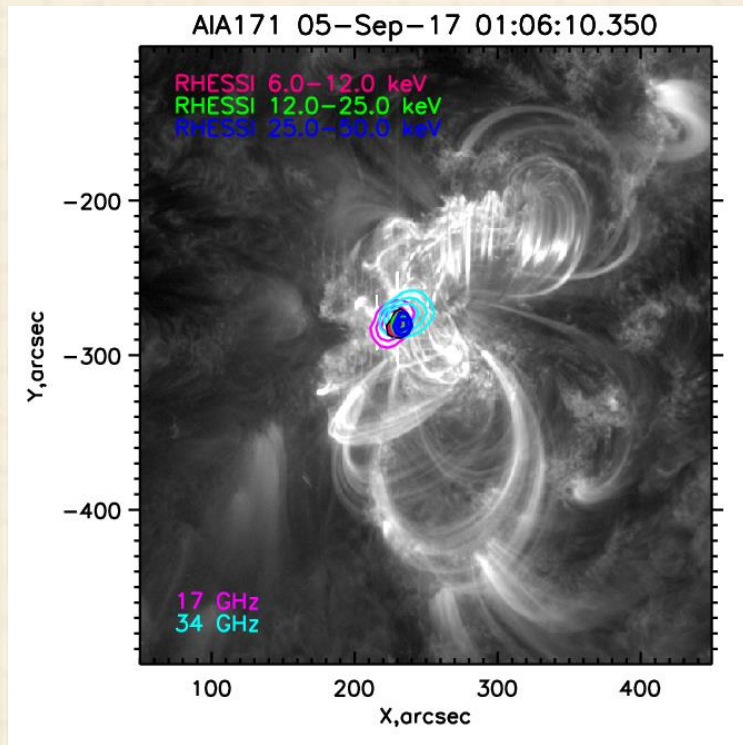


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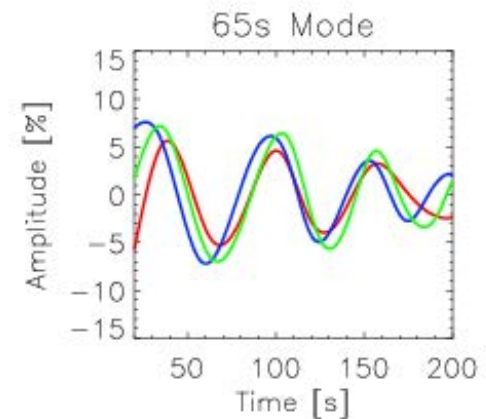
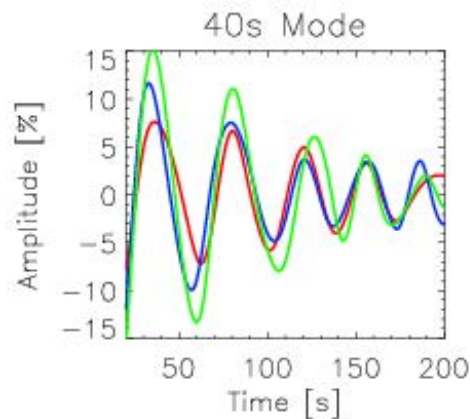
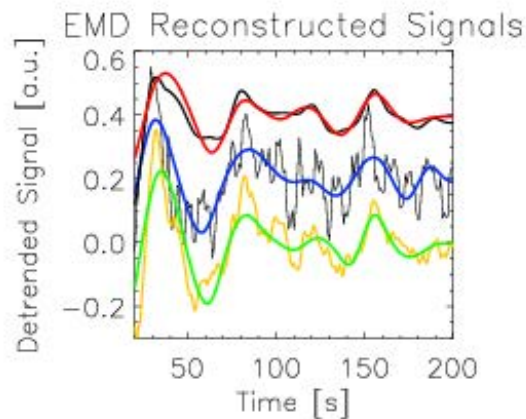
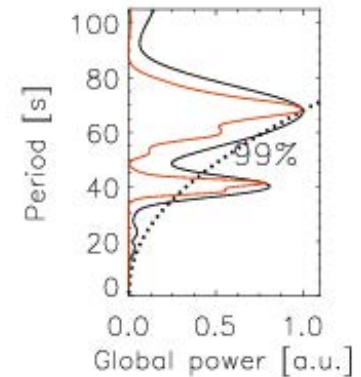
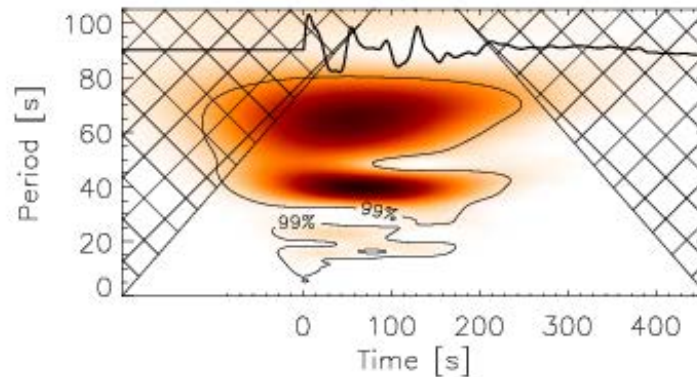
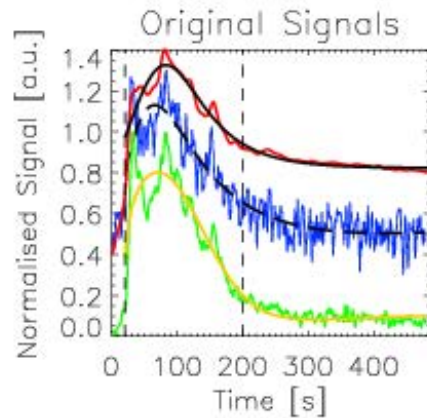
# Flare B: 05-Sep-2017 01:30 UT

## Multi-modal QPPs

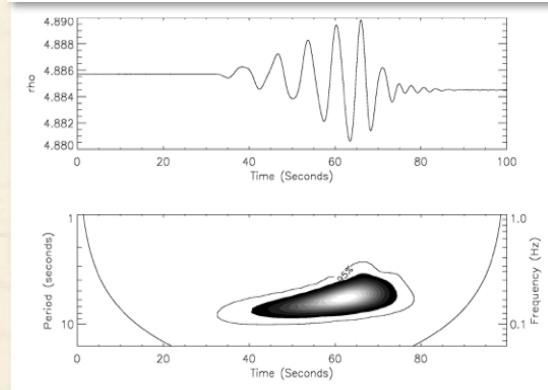
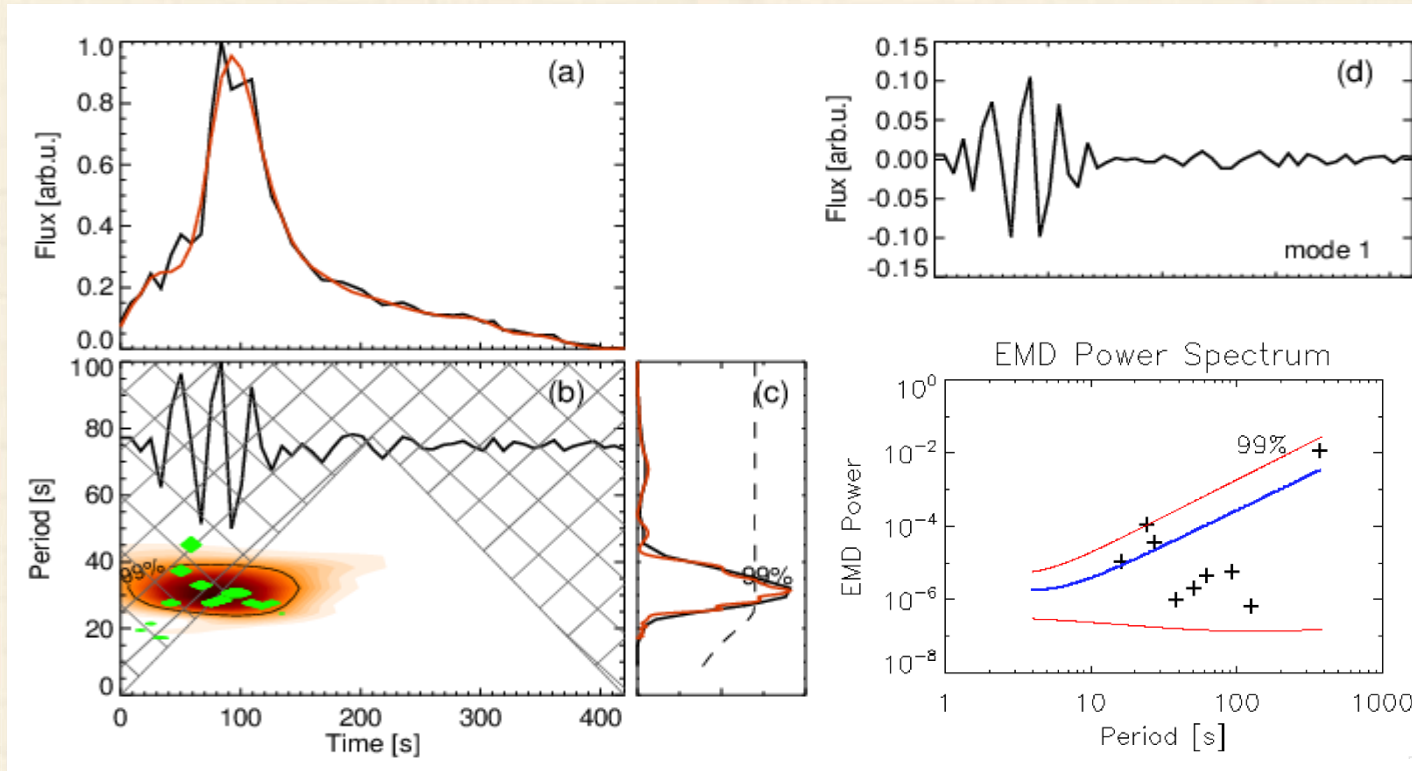


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## Multi-modal QPPs

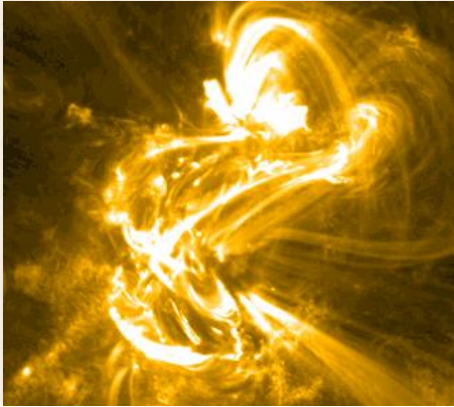


# Flare C: 05-Sep-2017 07:06 UT Natural non-stationarity.



Wavelet spectrum of "crazy tadpoles"  
(Nakariakov et al. 2004, MNRAS 349, 705).

# Flare C: 05-Sep-2017 07:06 UT Natural non-stationarity.

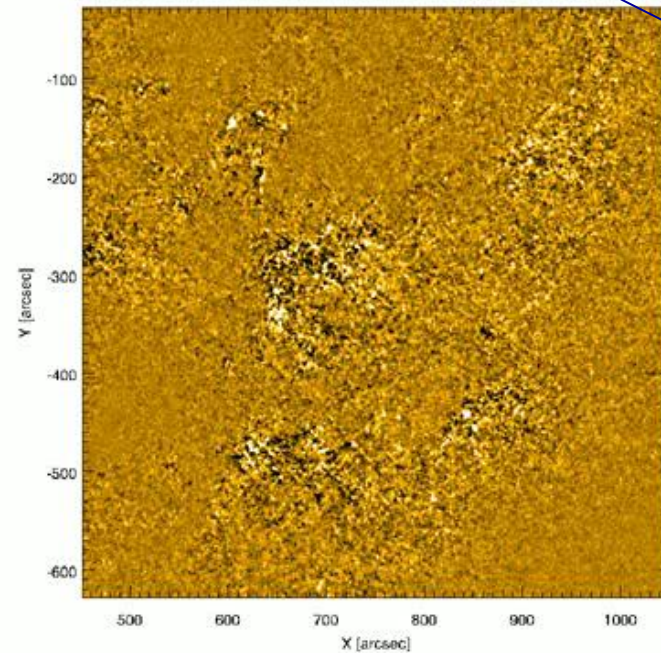
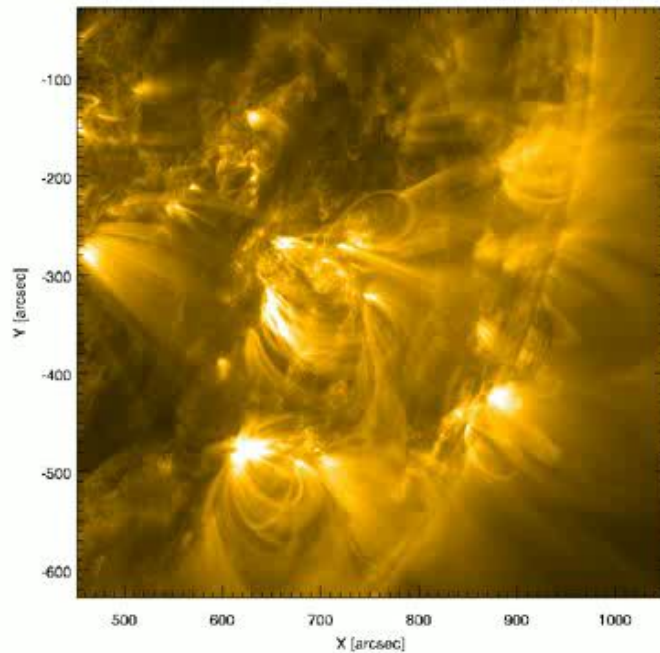


Propagating quasi-periodic waves of  
EUV intensity in lower corona

Nistico et al. A&A, 2014

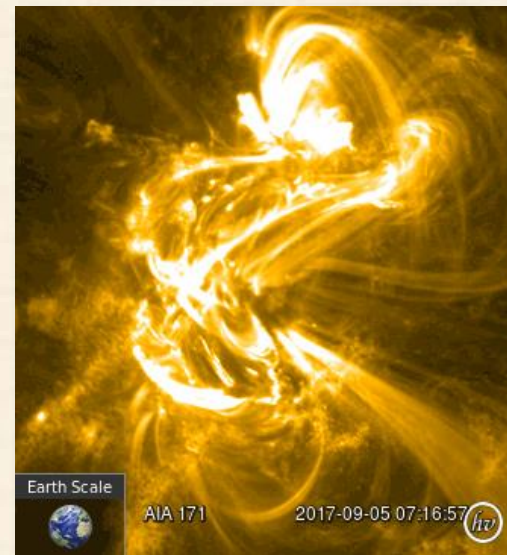
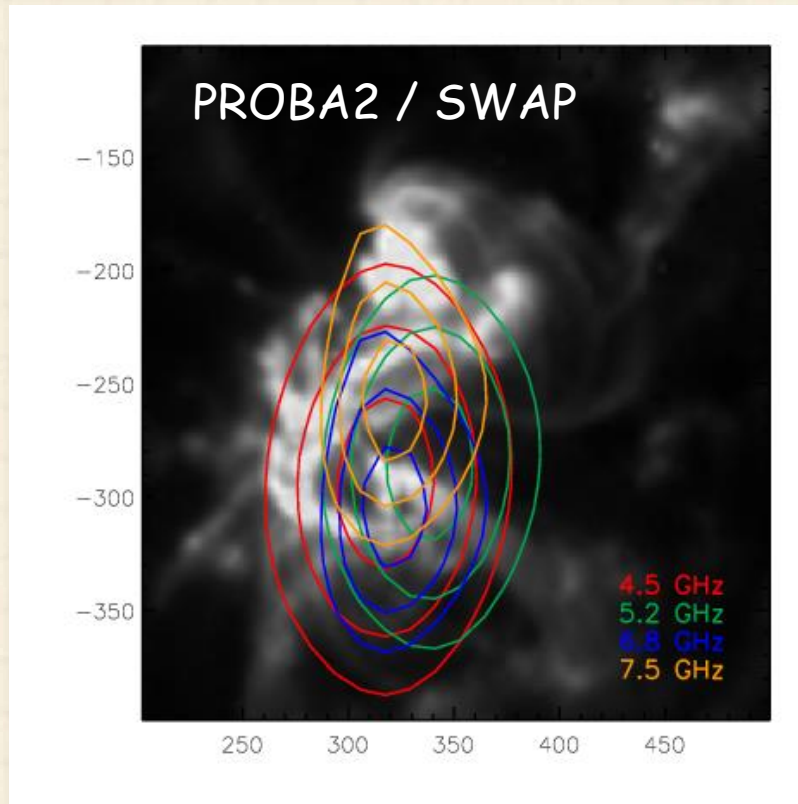
Also the talk by  
Leon Ofman yesterday

SDO/AIA 171 2013-12-07T07:00:23.34

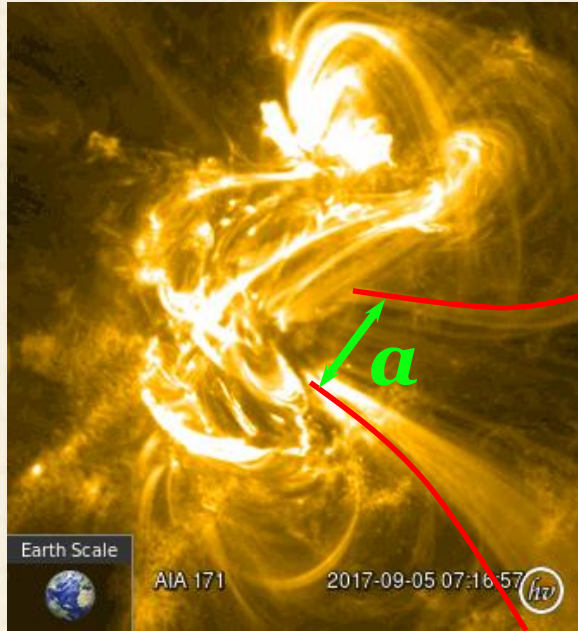




# Flare C: 05-Sep-2017 07:06 UT Natural non-stationarity.



# Flare C: 05-Sep-2017 07:06 UT Natural non-stationarity.



$a \approx 50'' \approx 36000 \text{ km}$

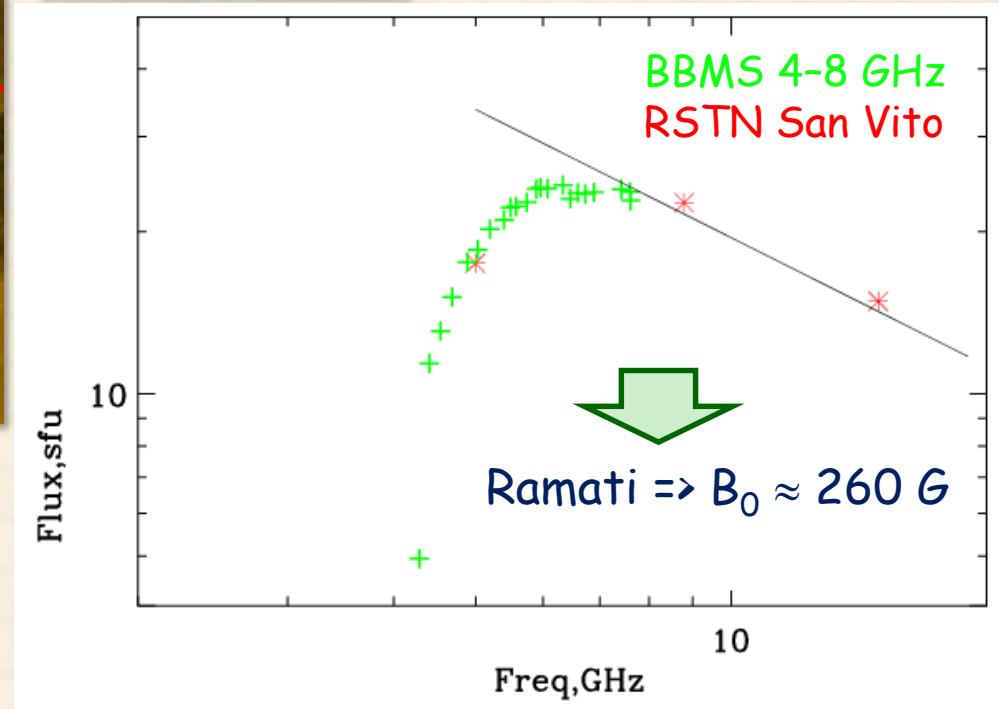
$P \approx 30 \text{ s}$



$v_A \approx 3200 \text{ km/s}$

$$P_1 \approx \frac{2.62a}{v_A}$$

Roberts et al. 1983, 1984  
Nakariakov et al. 2012



$B_0 = 260 \text{ G}$   
 $n_0 = 3 \cdot 10^{10} \text{ cm}^{-3}$   
 $v_A \approx 3300 \text{ km/s}$

$B_0 = 260 \text{ G}$   
 $n_0 = 10^{10} \text{ cm}^{-3}$   
 $v_A \approx 5700 \text{ km/s}$

# Conclusion

1. The non-stationary properties of QPPs are predicted by theory and they are observed by different instruments.
2. Two types of non-stationarity are introduced:
  1. natural non-stationarity associated with a time-dependent physical process
  2. the one appeared due to a multi-modal structure of QPPs
3. Methodic is under developing to detect and analyze the QPPs with non-stationary properties
4. Two solar flare are analyzed. Evidences are found of relation of the non-stationarity (the period shortening) to the propagating fast MHD mode.